

Redefining the axion window

Based on arXiv:1610.07593 In collaboration with [Luca Di Luzio](#) (IPPP, Durham) and [Federico Mescia](#) (Barcelona U.)

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Outline

- The strong CP problem: a short review
- Types of axion models, and the QCD axion
- Dark Matter from axion misalignment
- The window for preferred hadronic axion models
- Experimental searches

The strong CP problem

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- CP is expected to be violated in QCD:

$$\mathcal{L}_{\text{QCD}} = \sum_q \bar{q} (i\not{D} - m_q e^{i\theta_q}) q - \frac{1}{4} G_a^{\mu\nu} G_{\mu\nu}^a - \theta \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a$$

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- Only the difference $\bar{\theta} = \theta - \theta_q$ has physical meaning

$$q \rightarrow e^{i\gamma_5 \alpha} q \quad \longrightarrow \quad \theta_q \rightarrow \theta_q + 2\alpha \quad \text{and} \quad \theta \rightarrow \theta + 2\alpha$$

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- Change in θ is due to non invariance of path integral measure:

$$\mathcal{D}q\mathcal{D}\bar{q} \rightarrow \exp\left(-i\alpha \int d^4x \frac{\alpha_s}{4\pi} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a\right) \mathcal{D}q\mathcal{D}\bar{q}$$

[Fujikawa (1979)]

A small value problem

- $\bar{\theta} \neq 0$ implies a non-zero neutron EDM [Baluni (1979), Crewther et al. (1979)]

$$d_n \approx \frac{e |\bar{\theta}| m_\pi^2}{m_n^3} \approx 10^{-16} |\bar{\theta}| e \text{ cm}$$

- However, $d_n \lesssim 3 \cdot 10^{-26} e \text{ cm}$ implying:  $\bar{\theta} \lesssim 10^{-10}$

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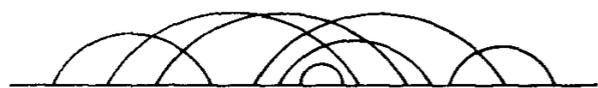


Fig. 9. Generic topology of a class of divergent CP violating 14th-order diagrams in the Kobayashi-Maskawa model [21,22].

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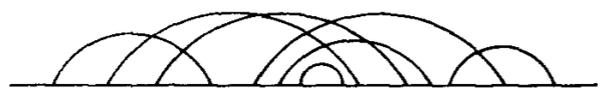


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- Unlike $y_{e,u,d} \sim 10^{-6} \div 10^{-5}$ it evades explanations based on environmental selection

[Ubaldi, 08 | I.1599]

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- From lattice: $m_u \neq 0$ by more than 20σ

[Aoki (2013)]

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 - Set $\bar{\theta} = 0$ by imposing CP. Need to break spont. for CKM (+BAU)
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 - Assume a global $U(1)_{PQ}$: (i) spontaneously broken; (ii) QCD anomalous
 - Implies a PGB of $U(1)_{PQ}$: the Axion. Shift symmetry: $a(x) \rightarrow a(x) + \delta\alpha f_a$

$$\mathcal{L}_{\text{eff}} = \left(\underbrace{\bar{\theta} + \frac{a}{f_a}}_{\theta_{\text{eff}}(x)} \right) \frac{\alpha_s}{8\pi} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a - \frac{1}{2} \partial^\mu a \partial_\mu a + \mathcal{L}(\partial_\mu a, \psi)$$

Relaxation of $\Theta_{\text{eff}}(x) \rightarrow 0$

- Minimum ground state energy in Euclidean V_4

$$e^{-V_4 E(\theta_{\text{eff}})} = \int \mathcal{D}\varphi e^{-S_0 + i\theta_{\text{eff}}\{G\tilde{G}\}} = \left| \int \mathcal{D}\varphi e^{-S_0 + i\theta_{\text{eff}}\{G\tilde{G}\}} \right| \leq \int \mathcal{D}\varphi \left| e^{-S_0 + i\theta_{\text{eff}}\{G\tilde{G}\}} \right| = e^{-V_4 E(0)}$$

[Vafa, Witten (1984)]

where $\{G\tilde{G}\} = \frac{\alpha_s}{8\pi} \int d^4x G^{\mu\nu} \tilde{G}_{\mu\nu}$, and using Schwartz inequality

- So $E(0) < E(\theta_{\text{eff}})$ and in the ground state the θ term is dynamically relaxed to 0.

Axion models

- **PQWW axion:**

Axion identified with the phase of the Higgs in a 2HDM
($f_a \sim V_{EW}$ was quickly ruled out long ago)

[Peccei, Quinn (1977),
Weinberg (1978), Wilczek (1978)]

The need to require $f_a \gg V_{EW}$: “invisible axion”

- **DSFZ Axion:** SM quarks and Higgs charged under PQ.

Requires 2HDM + 1 scalar singlet. SM leptons can also be charged.

[Dine, Fischler, Srednicki (1981), Zhitnitsky (1980)]

- **KSVZ axion** (or QCD axion, or hadronic axion):

All SM fields are neutral under PQ. QCD anomaly is induced by new quarks, vectorlike under the SM, chiral under PQ.

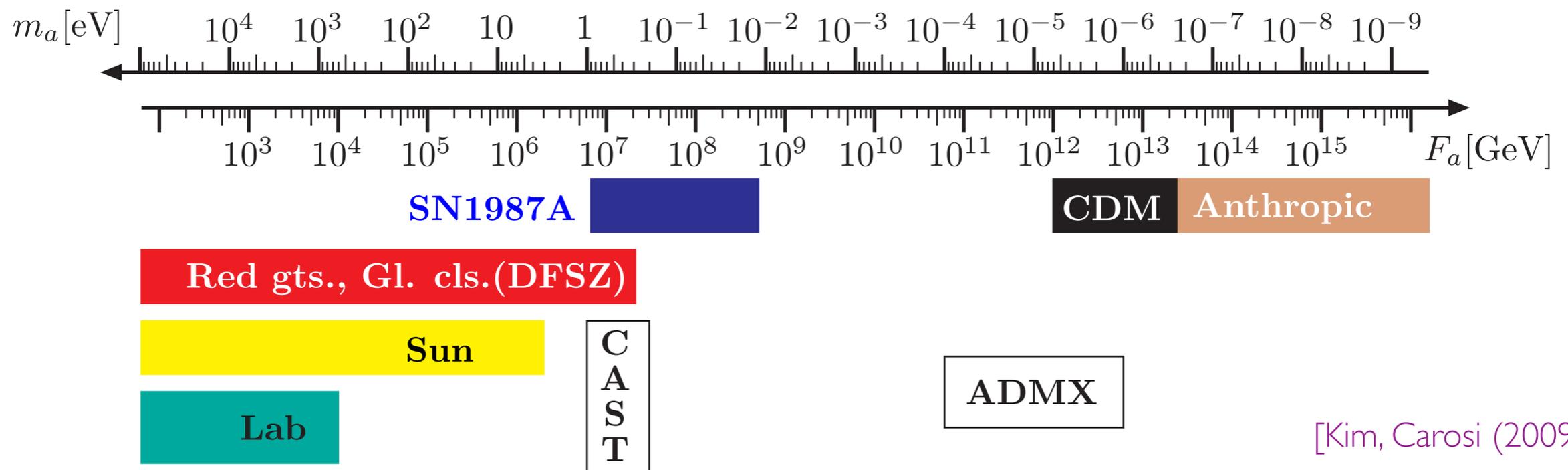
[Kim (1979), Shifman, Vainshtein, Sakharov (1980)]

Model independent features

- **Axion mass:** $\sim 1/f_a$ $m_a \simeq m_\pi \frac{f_\pi}{f_a} \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$
- **All axion couplings:** $\sim 1/f_a$

The lighter is the axion, the weaker are its interactions

Axion Landscape:



[Kim, Carosi (2009)]

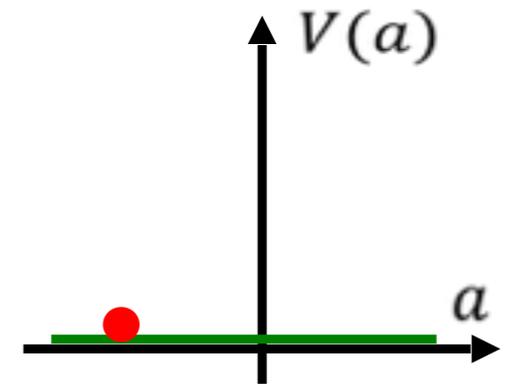
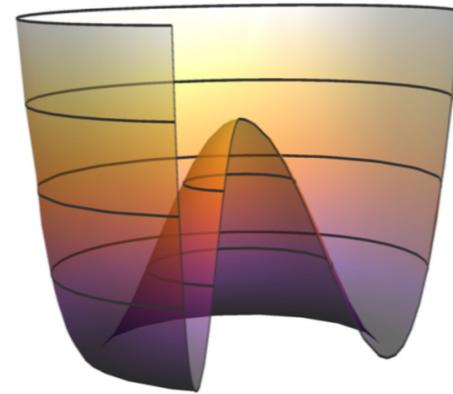
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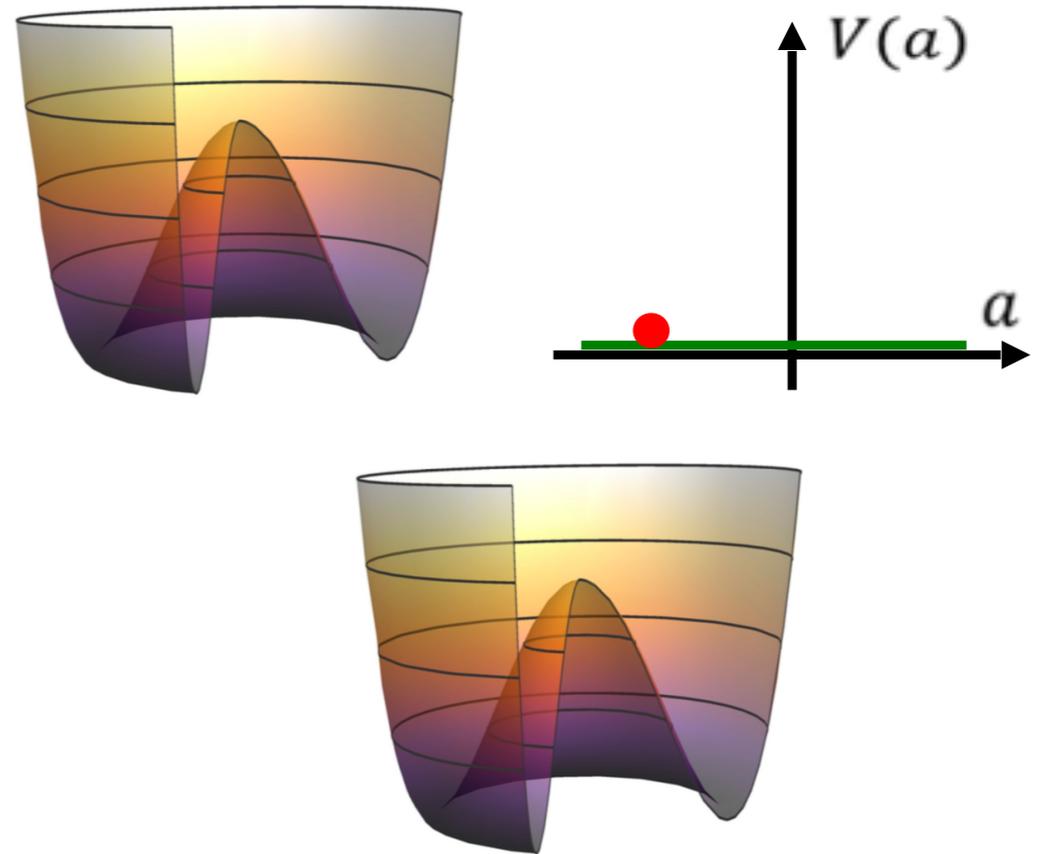
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$$\ddot{a} + 3H\dot{a} + \cancel{m_a^2(T)} f_a \sin\left(\frac{a}{f_a}\right) = 0$$

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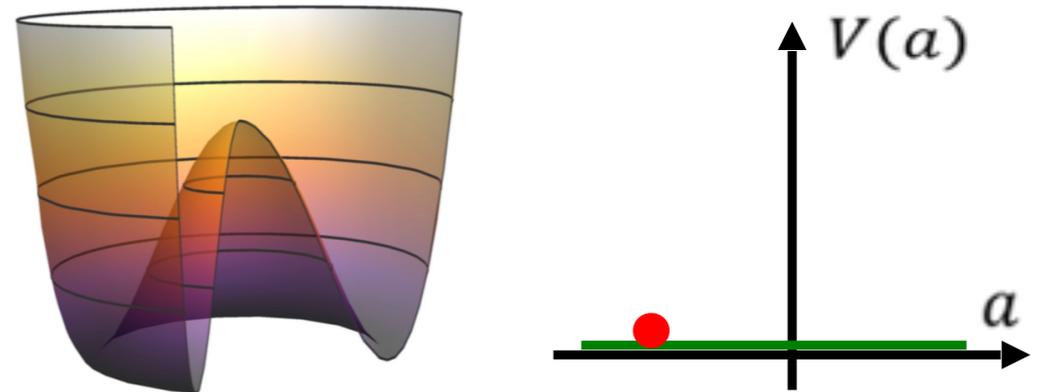
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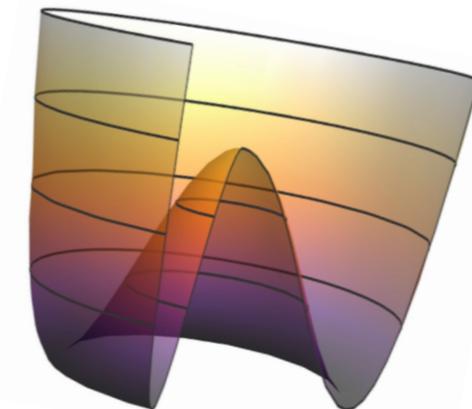
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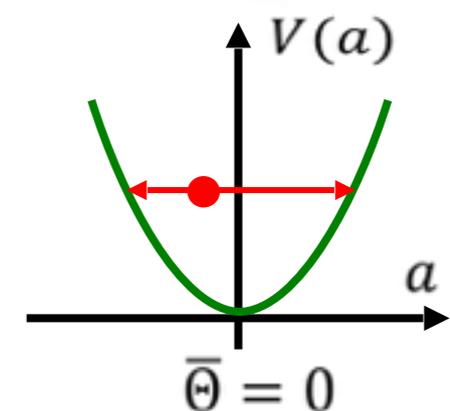
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 $m_a(T)$ turns on. When $m_a(T) > H \sim 10^{-9}$ eV,
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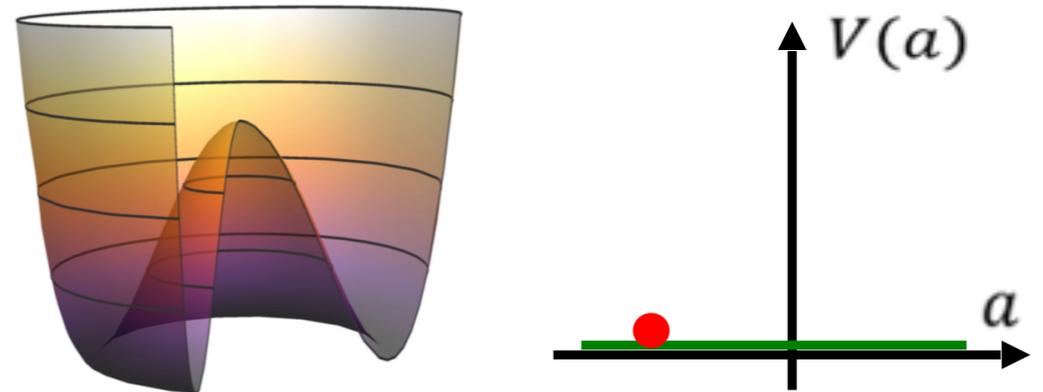


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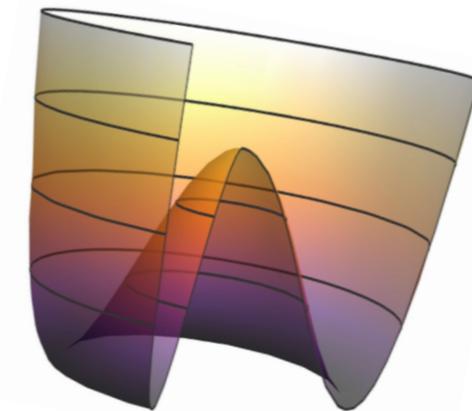


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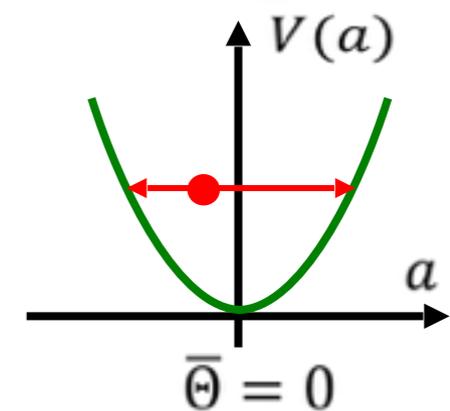
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- **Energy stored in oscillations behaves as CDM**

[Preskill, Wise, Wilczek (1983), Abbott, Sikivie (1983), Dine, Fischler (1983)]

Energy density & initial conditions

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- From recent lattice QCD calculations, [Bonati et al. 1512.06746, Petreczky et al. 1606.03145, Borsanyi et al. 1606.07494]
for $\theta_0 = \mathcal{O}(1)$ upper limit $f_a \lesssim 10^{11-12} \text{ GeV}$

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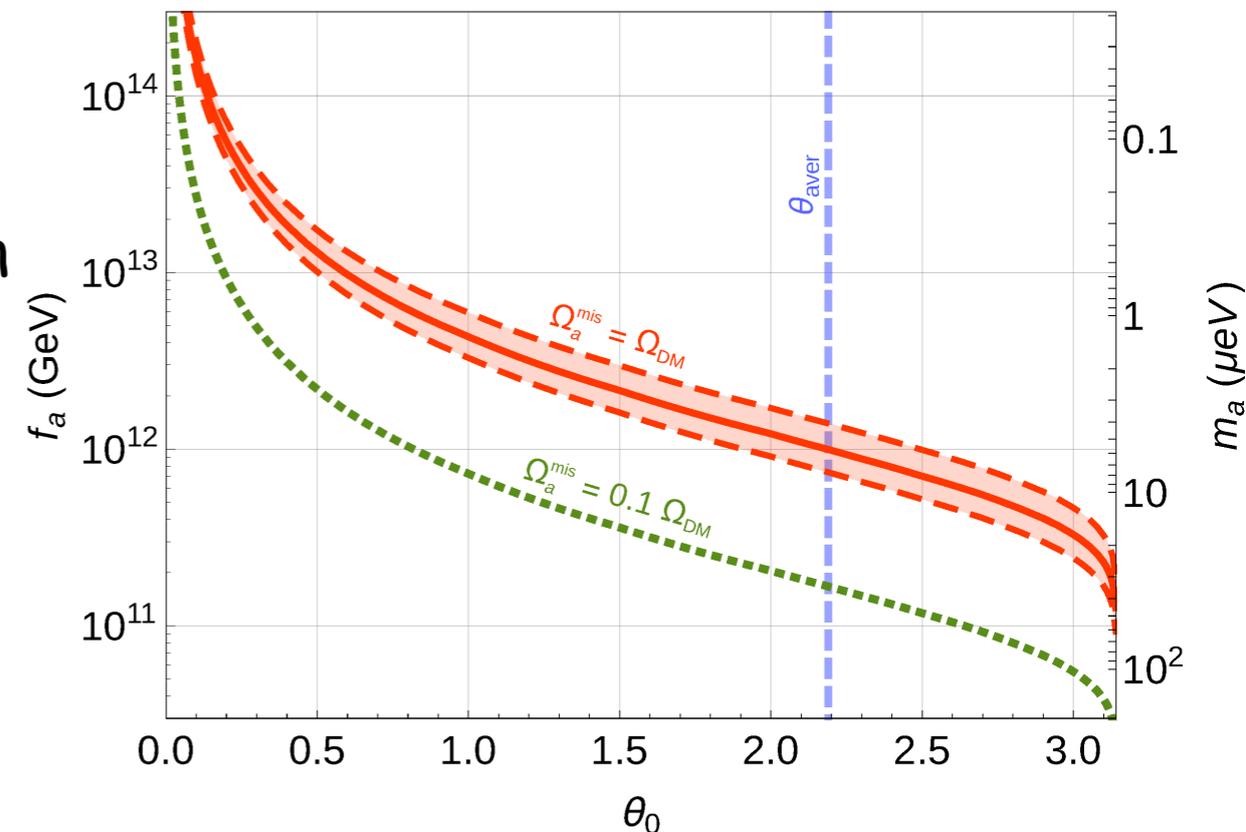
- From recent lattice QCD calculations, for $\theta_0 = \mathcal{O}(1)$ upper limit $f_a \lesssim 10^{11-12} \text{ GeV}$

- Value of θ_0 depends on the scale of inflation versus the PQ breaking scale f_a

– $U(1)_{\text{PQ}}$ broken after inflation: average over several Universe patches : $\langle \theta_0 \rangle = \pi/\sqrt{3}$

– $U(1)_{\text{PQ}}$ broken before inflation: in the whole observable Universe the same random value of θ_0

– “Anthropic Axion”: $f_a \gg 10^{12} \text{ GeV}$ is allowed only if $\theta_0 \ll 1$



Astrophysical lower limit on f_a

- **Astrophysical bounds**

[For a collection see e.g. Raffelt, hep-ph/0611350]

- Star evolution, RG lifetime

$$g_{a\gamma\gamma} \lesssim 6.6 \times 10^{-11} \text{ GeV}^{-1}$$

- White dwarf cooling

$$g_{aee} \lesssim 1.3 \times 10^{-13} \text{ GeV}^{-1}$$

- Supernova SN1987A

$$g_{aNN} \lesssim 3 \times 10^{-7} \text{ GeV}^{-1} \quad \longrightarrow \quad f_a \gtrsim 2 \times 10^8 \text{ GeV}$$

New search strategies

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- **Some new search possibilities which do not depend on $g_{a\gamma\gamma}$**

- **Cosmic Axion Spin Precession Experiment (CASPEr).**

[Budker et al., I306.6089]

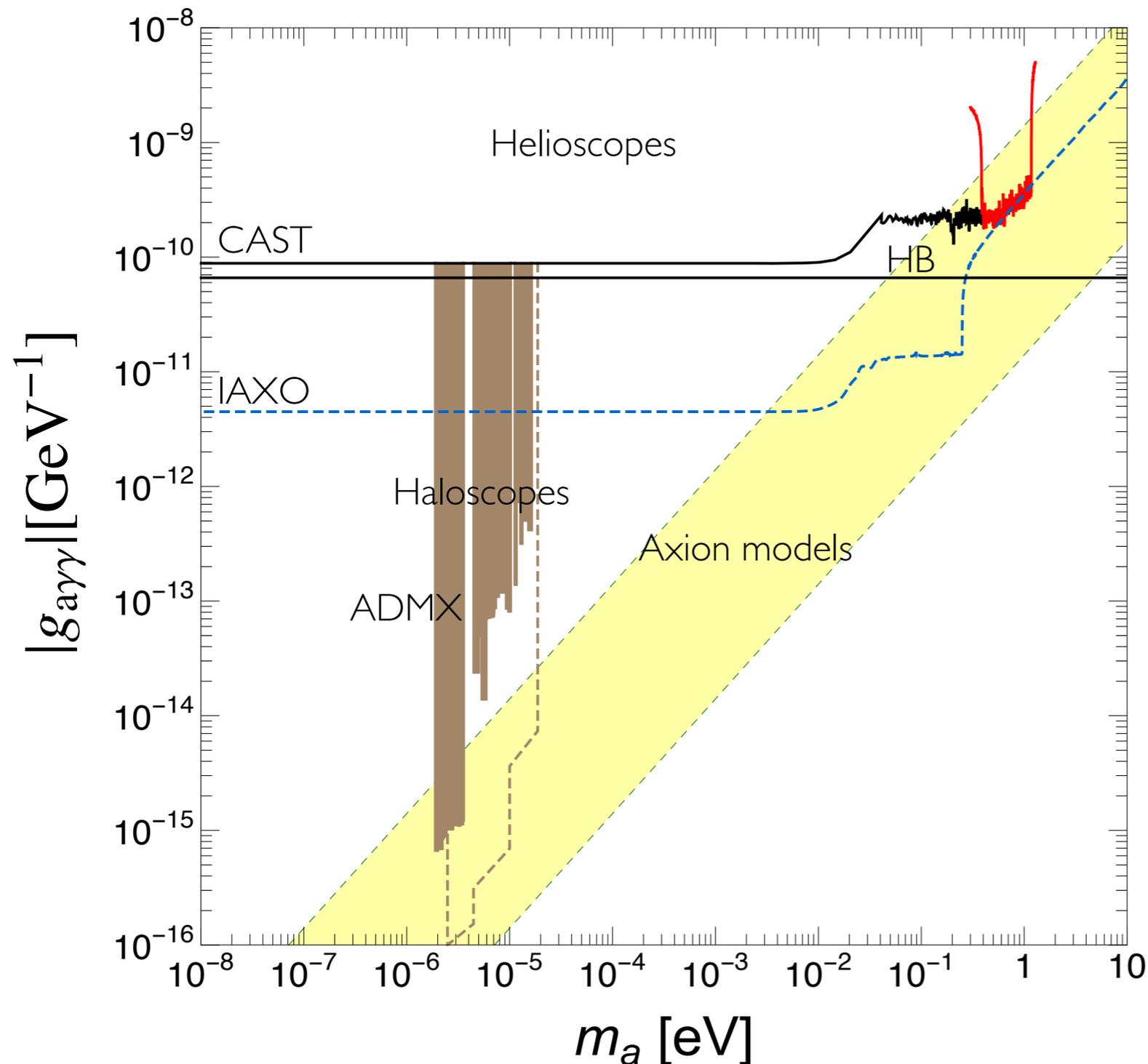
Background axion field might induce an oscillating neutron EDM, which can be detected via NMR techniques.

- **Black hole super-radiance (mainly bounds for ALPs)**

[Arvanitaki, Dubovsky I004.3558]

very light axions with a Compton wavelength comparable with that of a black hole can form a gravitational bound state and irradiate energy via gravitational waves

The "usual" axion window



$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92 \right)$$

$$|E/N - 1.92| \in [0.07, 7]$$

[Particle Data Group (since end of 90's).
Chosen to include some representative
models from: Kaplan, NPB 260 (1985),
Cheng, Geng, Ni, PRD 52 (1995),
Kim, PRD 58 (1998)]

Hadronic axions (KSVZ)

- Field content KSVZ

Field	Spin	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{PQ}$
Q_L	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_L
Q_R	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_R
Φ	0	1	1	0	1

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- PQ charges carried by SM-vectorlike quarks $Q = Q_L + Q_R$

- Original model assumes $Q \sim (3, 1, 0)$ [only $\mathcal{C}_Q \neq I$ is in fact required].

However in general:

$$\partial^\mu J_\mu^{PQ} = \frac{N\alpha_s}{4\pi} G \cdot \tilde{G} + \frac{E\alpha}{4\pi} F \cdot \tilde{F}$$

$$\left. \begin{aligned} N &= \sum_Q (\mathcal{X}_L - \mathcal{X}_R) T(\mathcal{C}_Q) \\ E &= \sum_Q (\mathcal{X}_L - \mathcal{X}_R) Q_Q^2 \end{aligned} \right\} \text{anomaly coeff.}$$

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- and by SM singlet Φ containing the "invisible" axion ($V_a \gg v_{EW}$)

$$\Phi(x) = \frac{1}{\sqrt{2}} [\rho(x) + V_a] e^{ia(x)/V_a}$$

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- Generic QCD axion Lagrangian: $\mathcal{L}_a = \mathcal{L}_{SM} + \mathcal{L}_{PQ} - V_{H\Phi} + \mathcal{L}_{Qq} \quad |\mathcal{X}_L - \mathcal{X}_R| = 1$

- $\mathcal{L}_{PQ} = |\partial_\mu \Phi|^2 + \bar{Q} i \not{D} Q - (y_Q \bar{Q}_L Q_R \Phi + \text{H.c.}) \quad \longrightarrow \quad m_Q = y_Q V_a / \sqrt{2}$

- $V_{H\Phi} = -\mu_\Phi^2 |\Phi|^2 + \lambda_\Phi |\Phi|^4 + \lambda_{H\Phi} |H|^2 |\Phi|^2 \quad \longrightarrow \quad m_\rho \sim V_a$

- \mathcal{L}_{Qq} : $d \leq 4$ couplings to SM quarks, depend on Q-gauge quantum numbers, but apparently also on their PQ charges

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- Symmetries of the gauge invariant kinetic term

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- Effective operators explicitly breaking $U(1)_Q$ and $U(1)_{PQ}$:

$$\mathcal{L}_{Qq}^{d>4} \longrightarrow \text{Can allow Q decays even if } \mathcal{L}_{Qq} = 0$$

Accidental symmetries

- Symmetries of the gauge invariant kinetic term

$$U(1)_{Q_L} \times U(1)_{Q_R} \times U(1)_\Phi \xrightarrow{y_Q \neq 0} U(1)_{PQ} \times U(1)_Q$$

$$\mathcal{L}_{PQ} = |\partial_\mu \Phi|^2 + \bar{Q} i \not{D} Q - (y_Q \bar{Q}_L Q_R \Phi + \text{H.c.})$$

- $U(1)_Q$ is Q-baryon number. Exact $U(1)_Q \Rightarrow$ Q stability. [E.g. $Q \sim (3,1,0)$]
- if $\mathcal{L}_{Qq} \neq 0$ $U(1)_Q \times U(1)_B$ is broken to 'extended' $U(1)_{B'}$. **Q's can decay**

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$$V_\Phi^{d>4} \ni \frac{\Phi^N}{M_{\text{Planck}}^{N-4}} \longrightarrow \text{If } N < 10 \text{ would spoil the PQ solution}$$

[Kamionkowski, March-Russell (1992), Holman et al. (1992), Barr, Seckel (1992)]

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$$Q_L \rightarrow Q_L, \quad Q_R \rightarrow \omega^{N-1} Q_R, \quad \Phi \rightarrow \omega \Phi, \quad \text{where} \quad \omega \equiv e^{i2\pi/N}$$

$\mathbb{Z}_N(q)$	$d \leq 4$	$d = 5$	$(\mathcal{X}_L, \mathcal{X}_R)$
1	$\bar{Q}_L d_R$	$\bar{Q}_L \gamma_\mu q_L (D^\mu H)^\dagger$	(0, -1)
ω	$\bar{Q}_L d_R \Phi^\dagger$		(-1, -2)
ω^{N-2}	–	$\bar{Q}_L d_R \Phi^2, \bar{Q}_R q_L H^\dagger \Phi$	(2, 1)
ω^{N-1}	$\bar{q}_L Q_R H, \bar{Q}_L d_R \Phi$	–	(1, 0)

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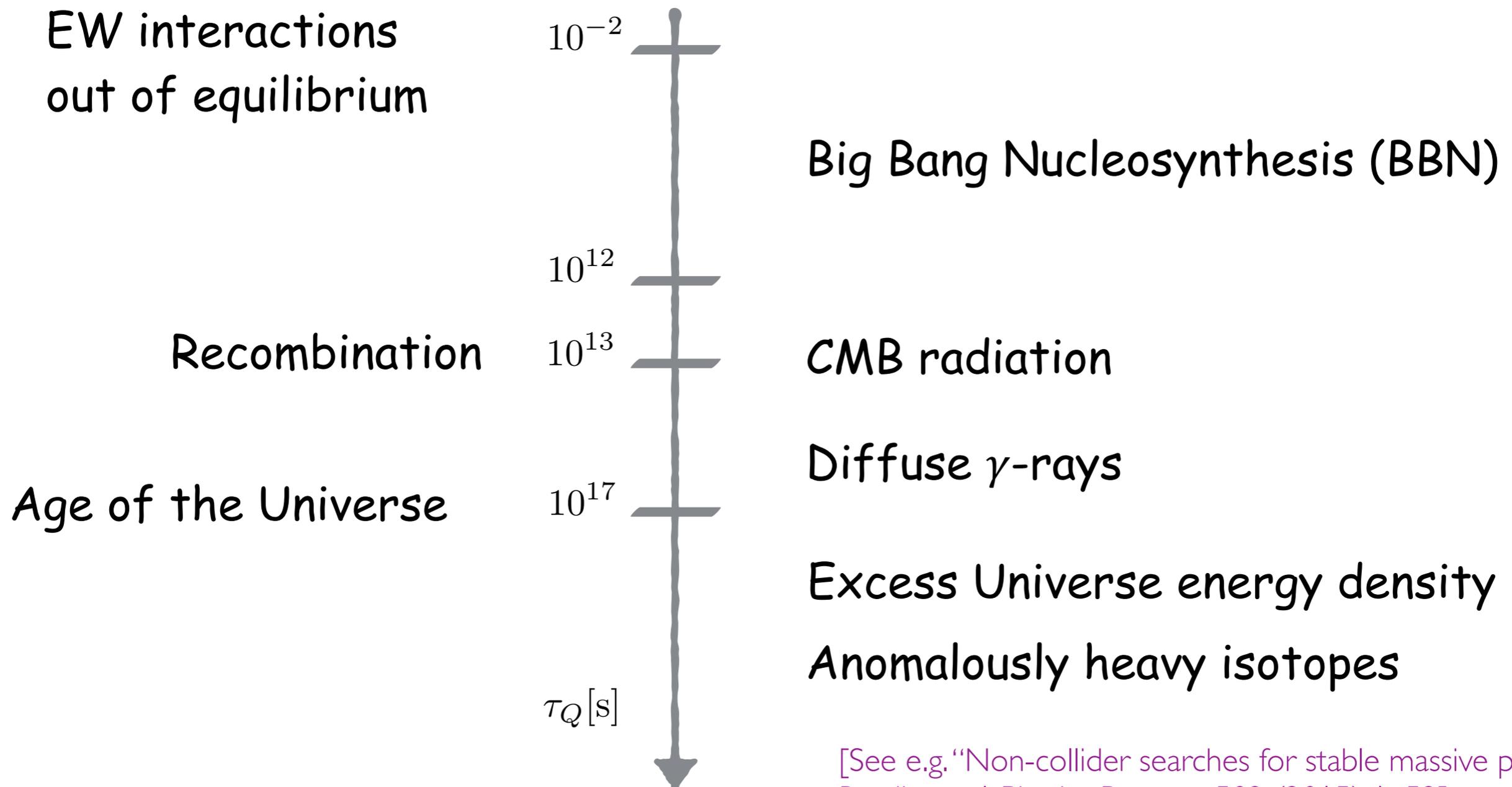
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Ensures that the min. dimension of the $U(1)_{PQ}$ breaking operators in $V_\Phi^{d>4}$ is N . The dim of the $U(1)_Q$ breaking opts. depends on $\mathbb{Z}_N(q)$

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Cosmological constraints on τ_Q

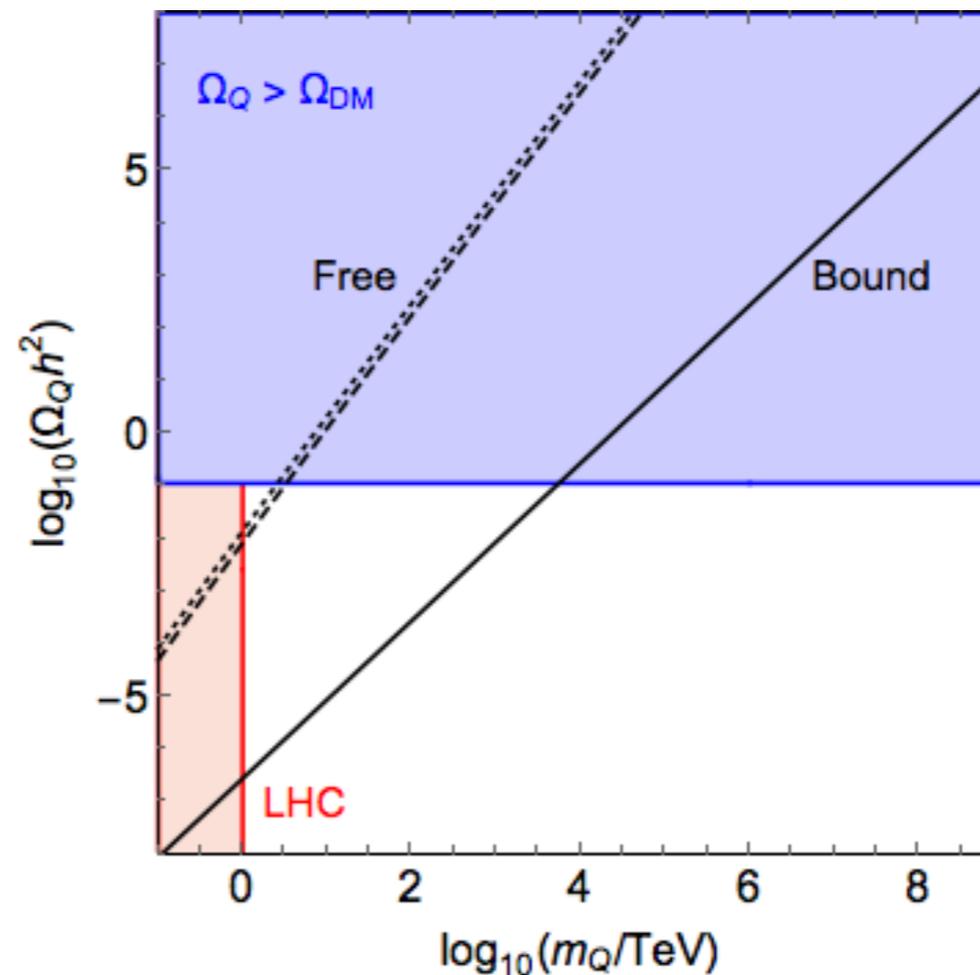
- Strongly interacting long-lived particles are an issue in cosmology



[See e.g. “Non-collider searches for stable massive particles”,
Burdin et al. Physics Reports 582 (2015) 1–52]

Cosmological constraints on τ_Q

- Assume $m_Q \ll T_{\text{reheating}}$ (thermal distribution of Q's as initial condition)
Free quark annihilation: excess $\Omega_Q > \Omega_{\text{DM}}$ would allow to exclude $\tau_Q \approx \tau_{\text{Univ}}$
- At $T < \Lambda_{\text{QCD}}$ bound state formation can catalyse annihilations.
E.g. for color triplets: $Q^*q + Qqq \rightarrow [Q^*Q] + qqq$
- However $QQ\dots$, QQQ bound bound states would hinder it.
- A reliable estimate of Ω_Q remains an open issue !



First selection criterium

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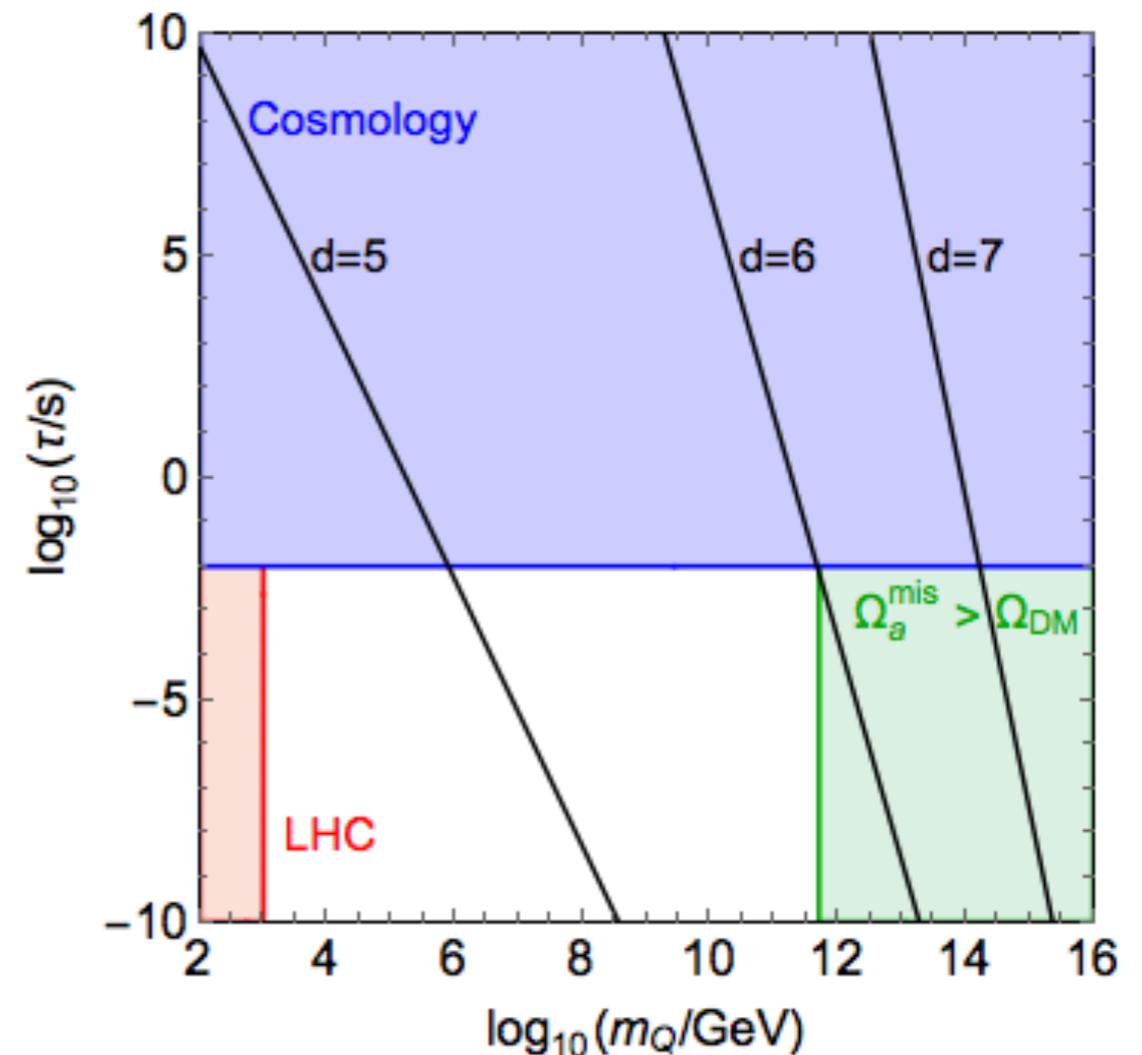
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- Decays via $d=4$ operators are always sufficiently fast.
- Decays via higher order operators are fast enough only for $d=5$ and $m_Q \gtrsim 800$ TeV.

$$\mathcal{L}_{Qq}^{d>4} = \frac{1}{M_{\text{Planck}}^{(d-4)}} \mathcal{O}_{Qq}^{d>4} + \text{h.c.}$$

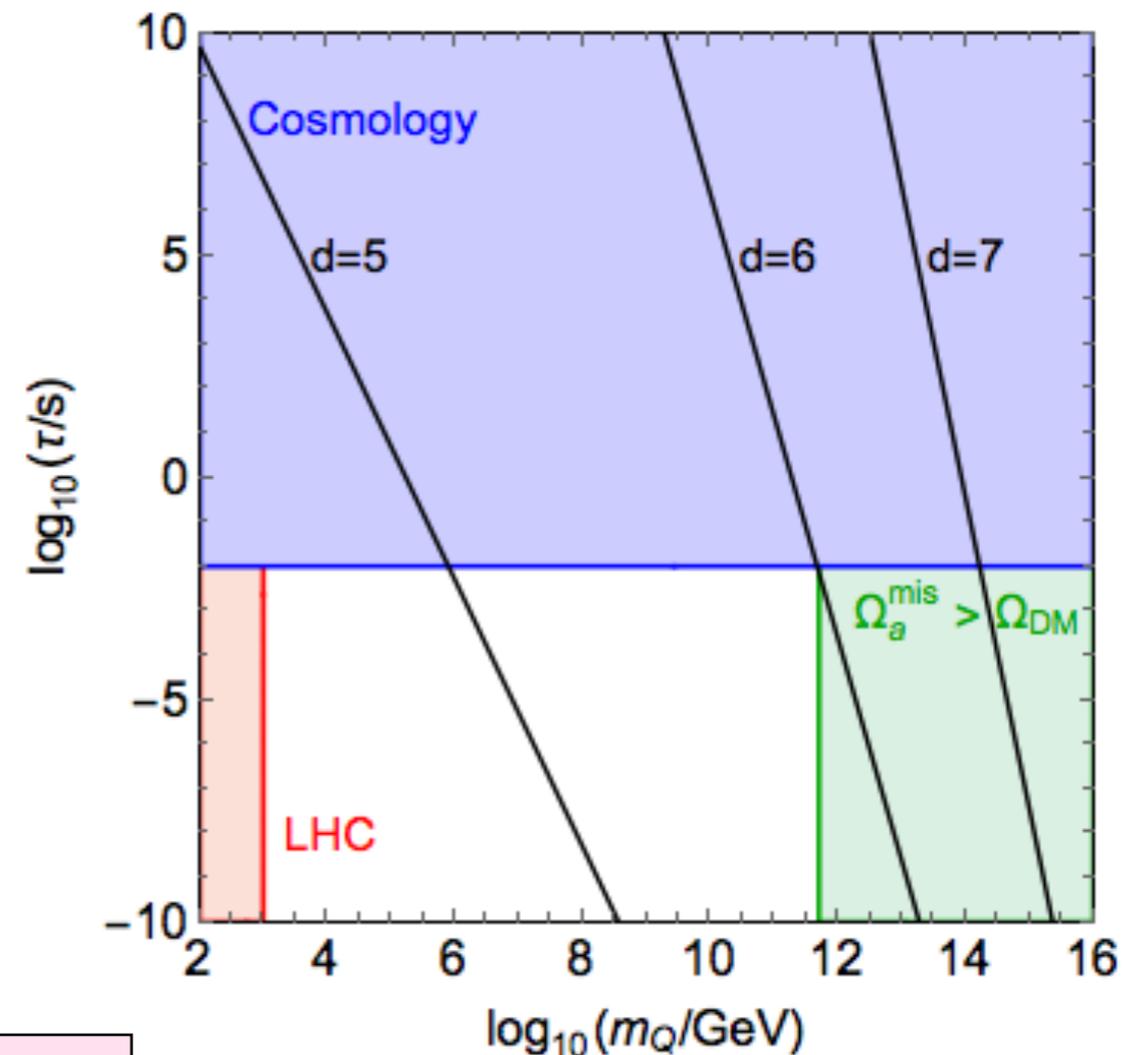


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→ Therefore, "safe" R(Q) must allow for gauge invariant d=4 or d=5 operators

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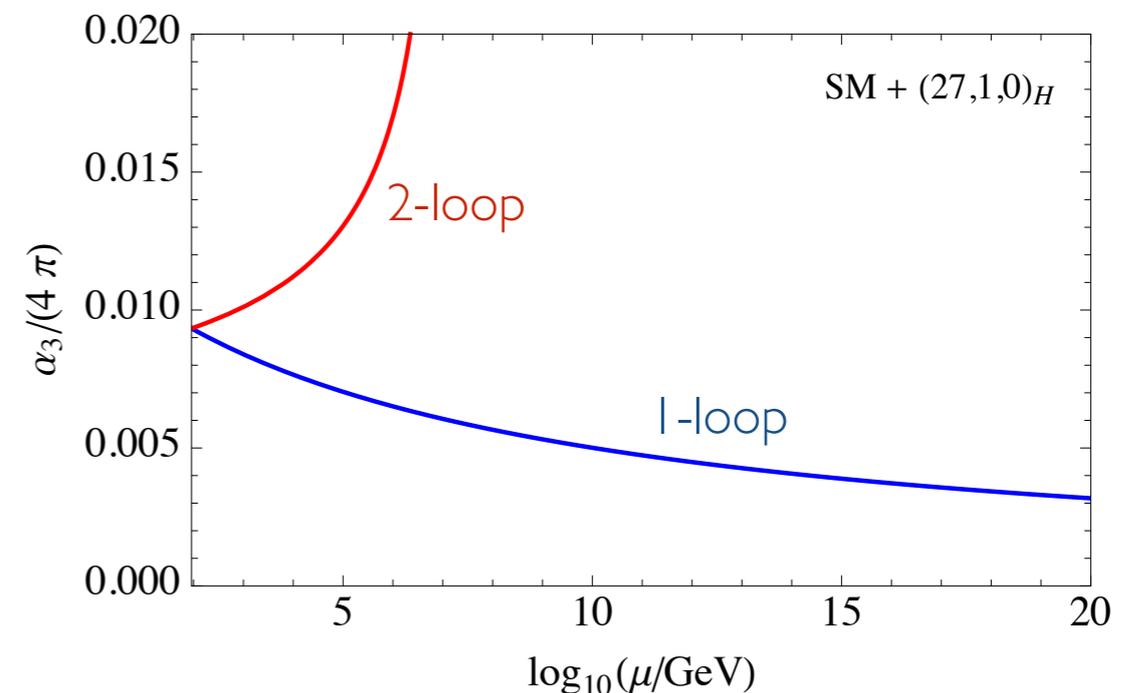
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Two-loop β functions help to avoid spurious results from accidental cancellations in 1-loop β functions...

[Di Luzio, Gröber, Kamenik, Nardecchia, 1504.00359]



Phenomenologically preferred Q's

$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92(4) \right)$$

$$\frac{E}{N} = \frac{\sum_Q \mathcal{Q}_Q^2}{\sum_Q T(\mathcal{C}_Q)}$$

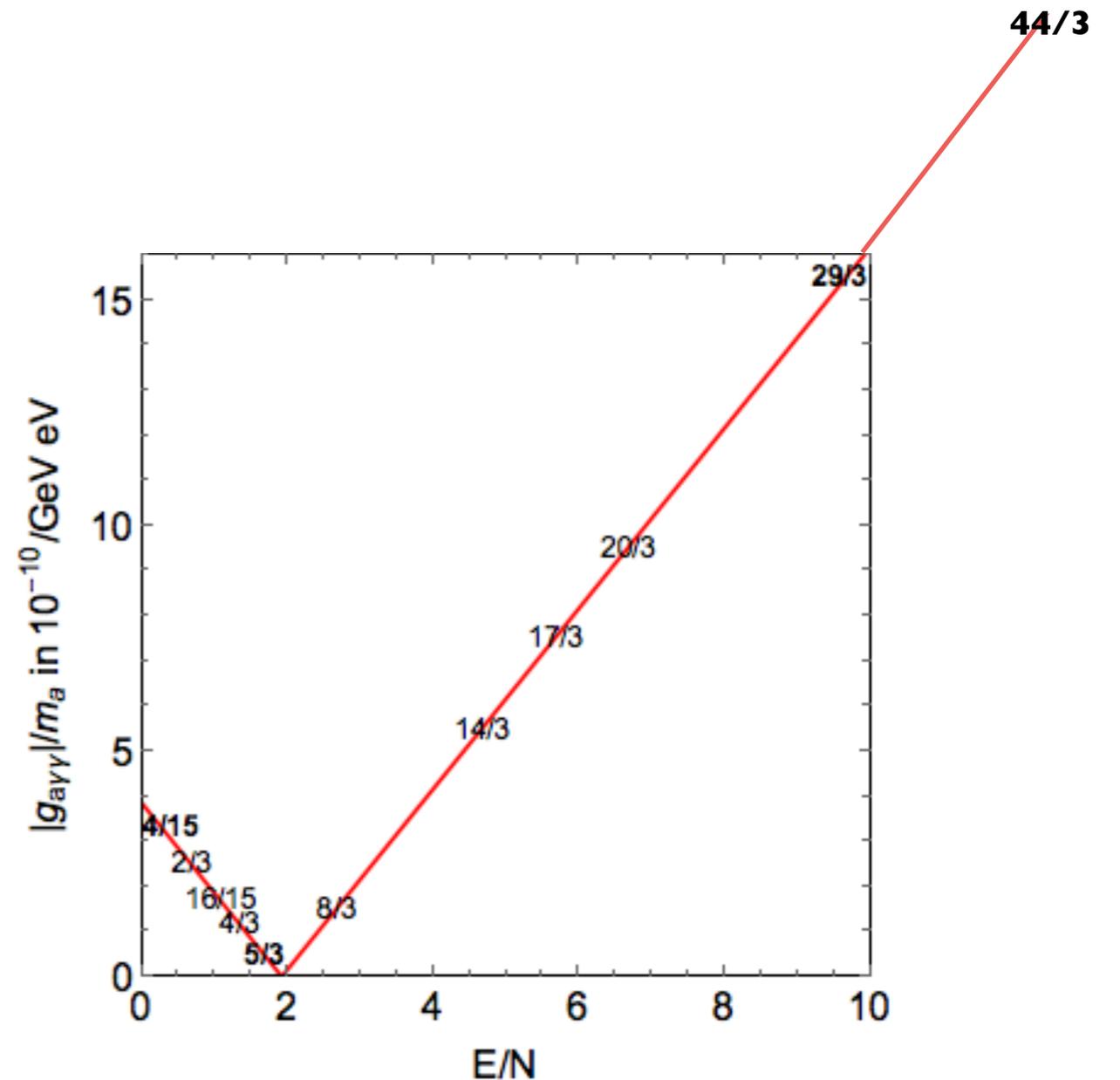
R_Q	\mathcal{O}_{Qq}	$\Lambda_{\text{Landau}}^{2\text{-loop}} [\text{GeV}]$	E/N
(3, 1, -1/3)	$\bar{Q}_L d_R$	$9.3 \cdot 10^{38} (g_1)$	2/3
(3, 1, 2/3)	$\bar{Q}_L u_R$	$5.4 \cdot 10^{34} (g_1)$	8/3
(3, 2, 1/6)	$\bar{Q}_R q_L$	$6.5 \cdot 10^{39} (g_1)$	5/3
(3, 2, -5/6)	$\bar{Q}_L d_R H^\dagger$	$4.3 \cdot 10^{27} (g_1)$	17/3
(3, 2, 7/6)	$\bar{Q}_L u_R H$	$5.6 \cdot 10^{22} (g_1)$	29/3
(3, 3, -1/3)	$\bar{Q}_R q_L H^\dagger$	$5.1 \cdot 10^{30} (g_2)$	14/3
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(3, 3, -4/3)	$\bar{Q}_L d_R H^{\dagger 2}$	$3.5 \cdot 10^{18} (g_1)$	44/3
($\bar{6}$, 1, -1/3)	$\bar{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$2.3 \cdot 10^{37} (g_1)$	4/15
($\bar{6}$, 1, 2/3)	$\bar{Q}_L \sigma_{\mu\nu} u_R G^{\mu\nu}$	$5.1 \cdot 10^{30} (g_1)$	16/15
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(8, 1, -1)	$\bar{Q}_L \sigma_{\mu\nu} e_R G^{\mu\nu}$	$7.6 \cdot 10^{22} (g_1)$	8/3
(8, 2, -1/2)	$\bar{Q}_R \sigma_{\mu\nu} \ell_L G^{\mu\nu}$	$6.7 \cdot 10^{27} (g_1)$	4/3
(15, 1, -1/3)	$\bar{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$8.3 \cdot 10^{21} (g_3)$	1/6
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Phenomenologically preferred Q's

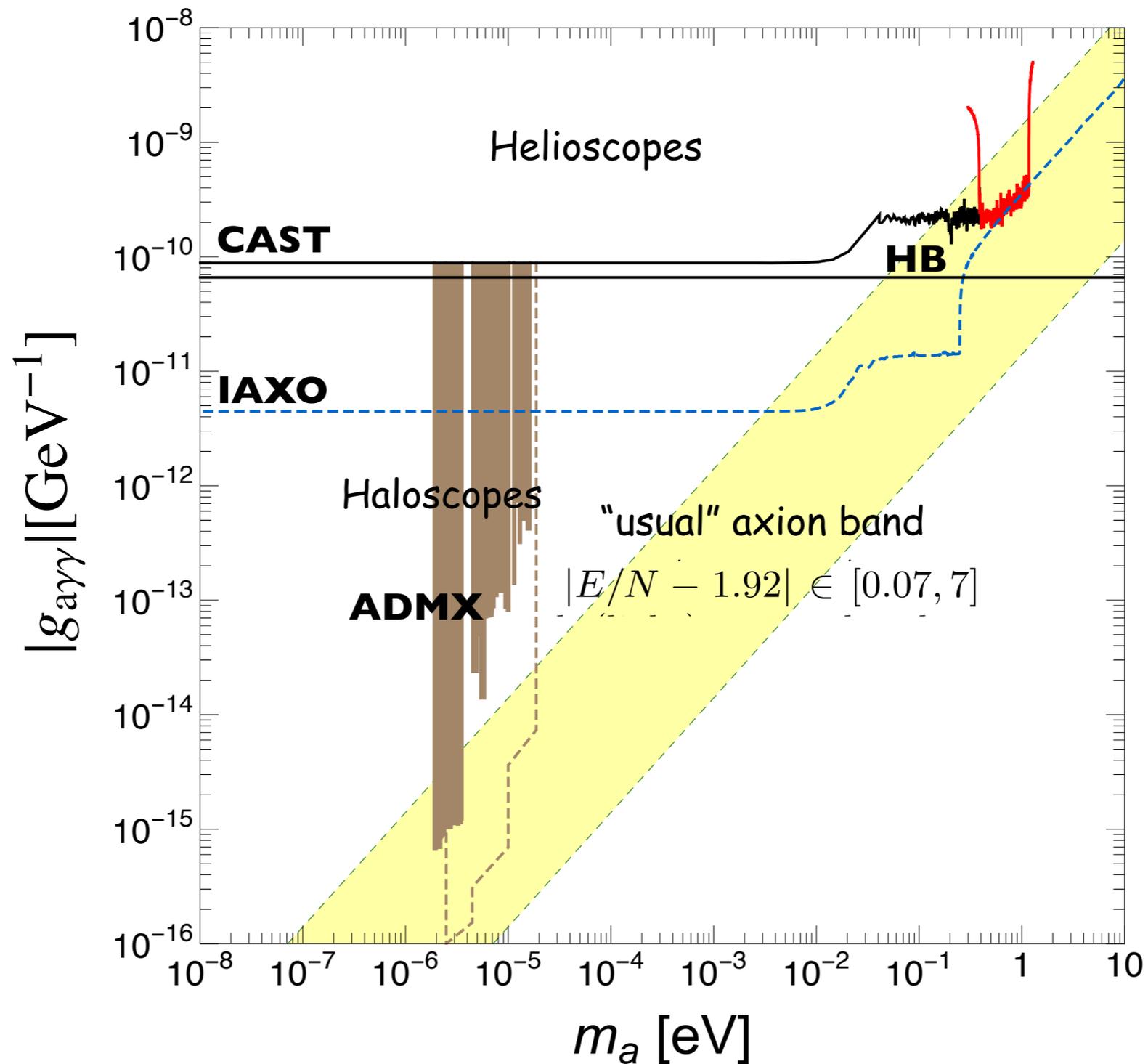
- Only 15 Q's survive:

	R_Q	\mathcal{O}_{Qq}	$\Lambda_{\text{Landau}}^{2\text{-loop}} [\text{GeV}]$	E/N
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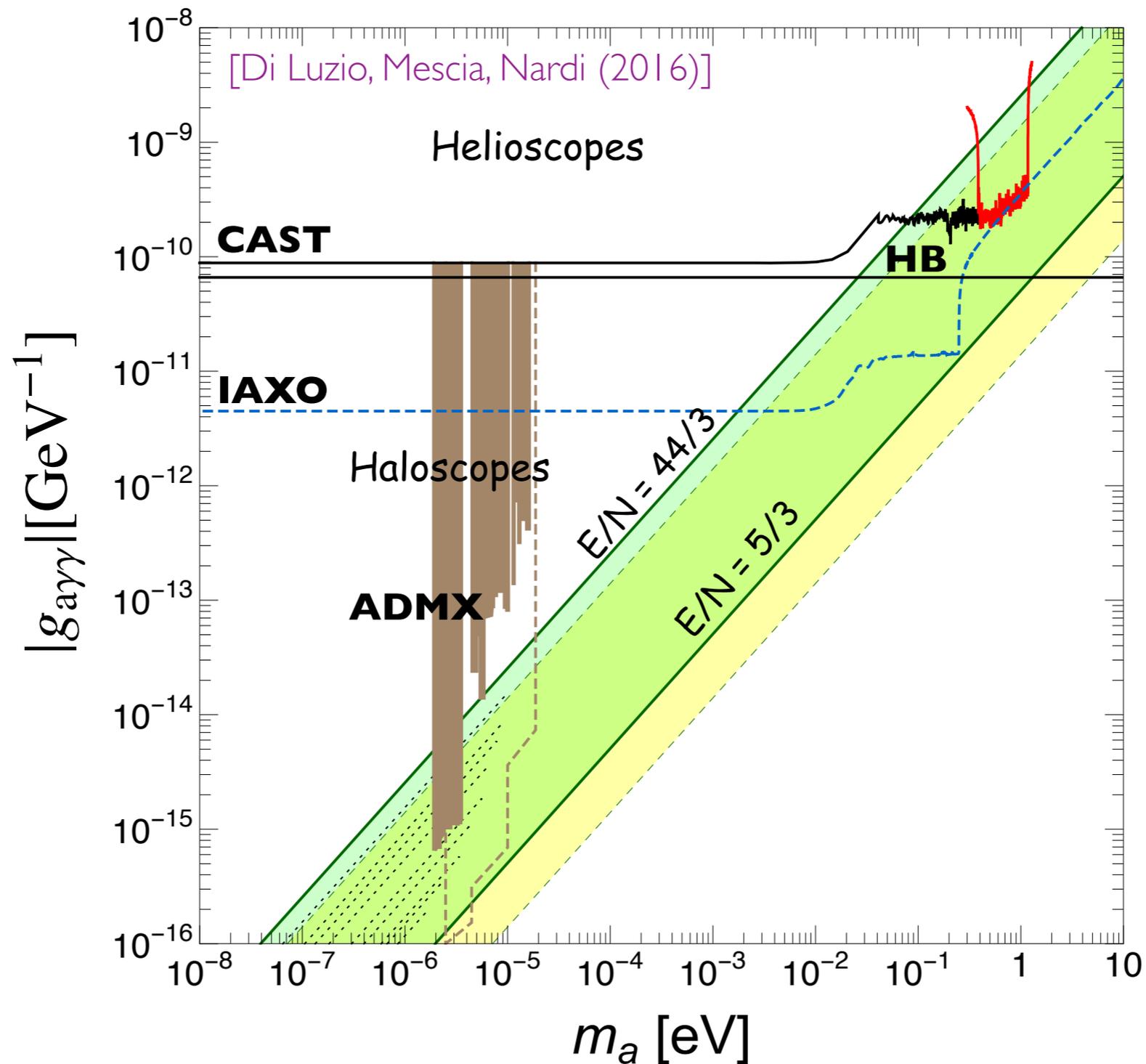
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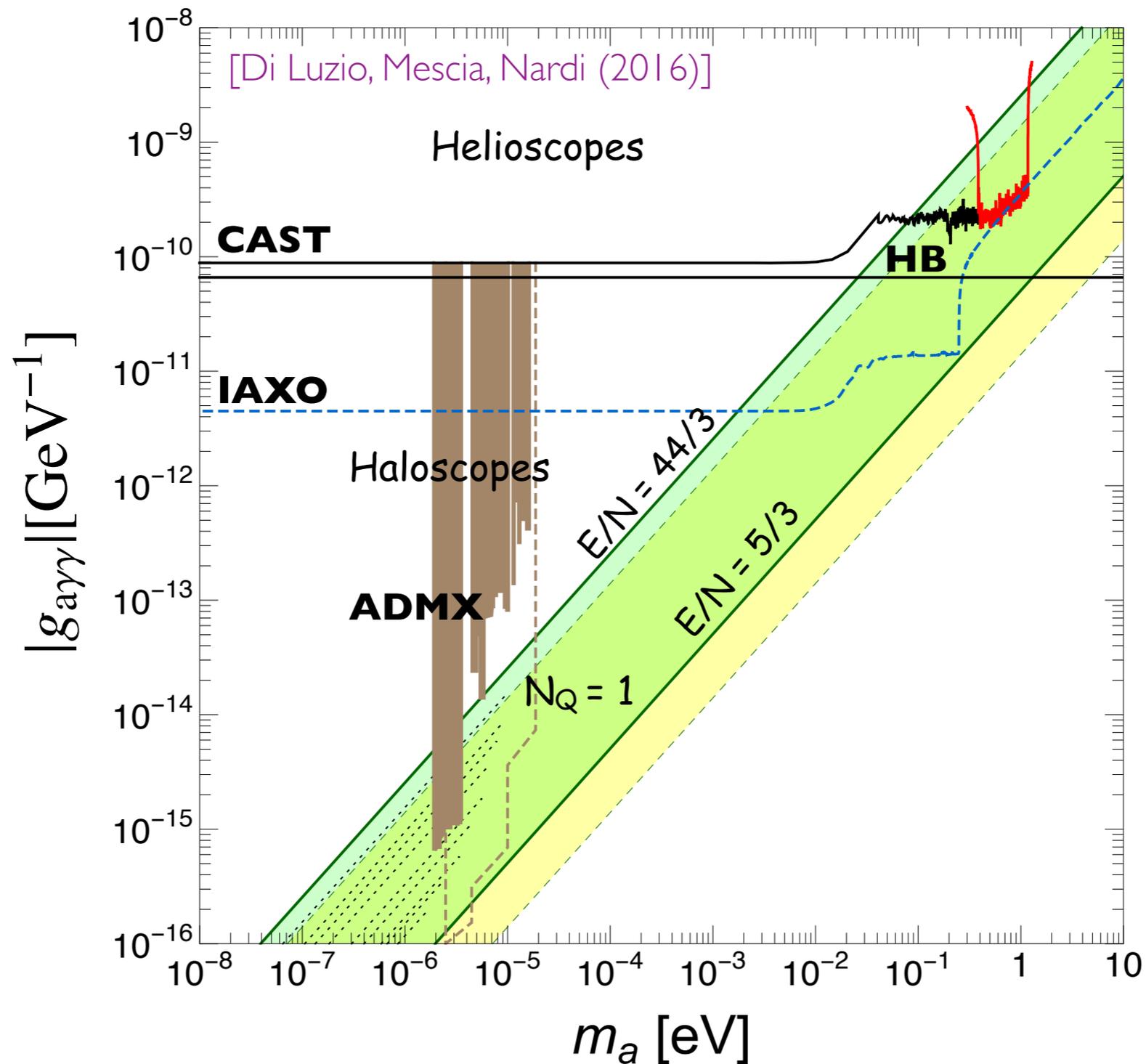
Redefining the axion window



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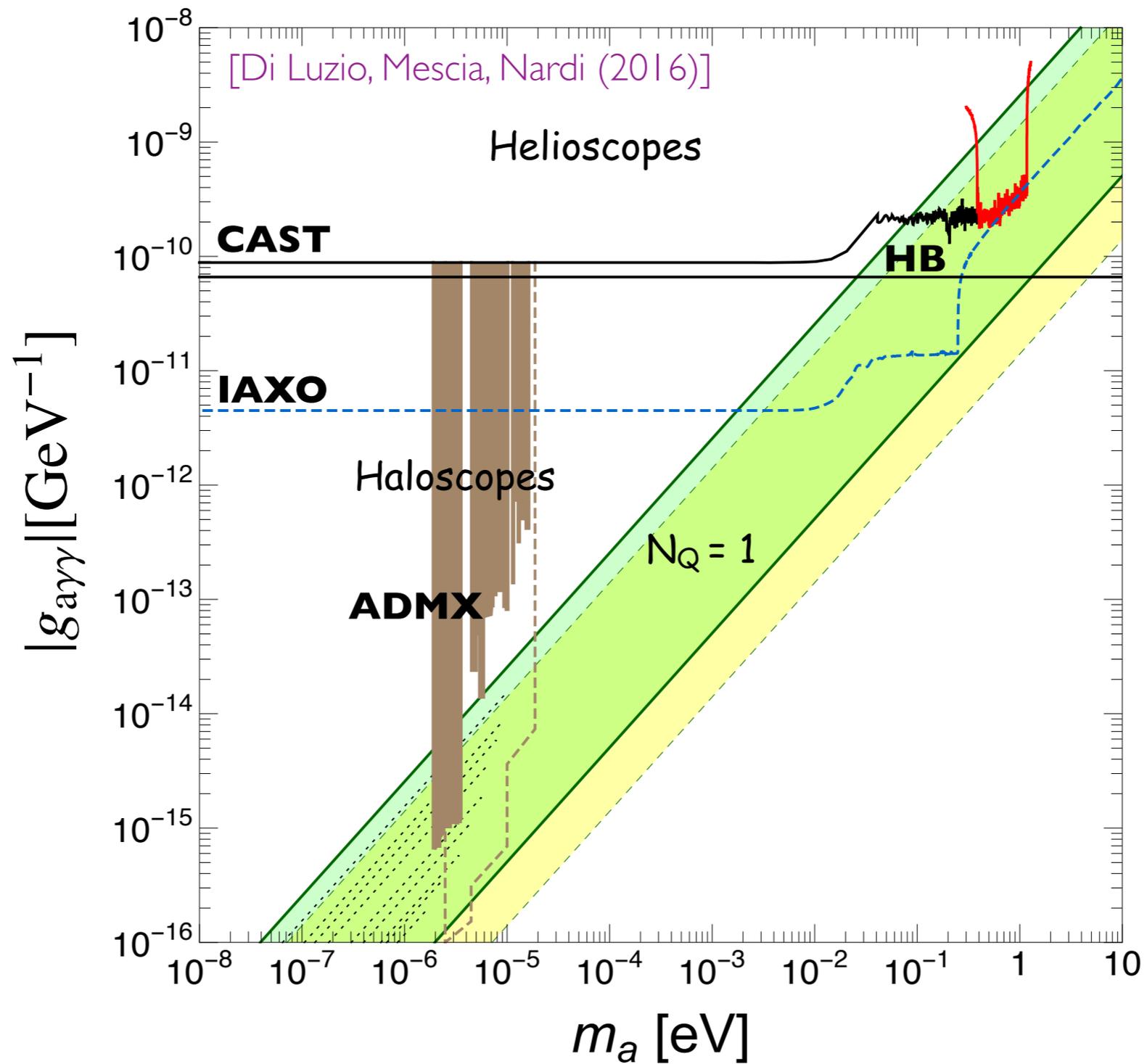
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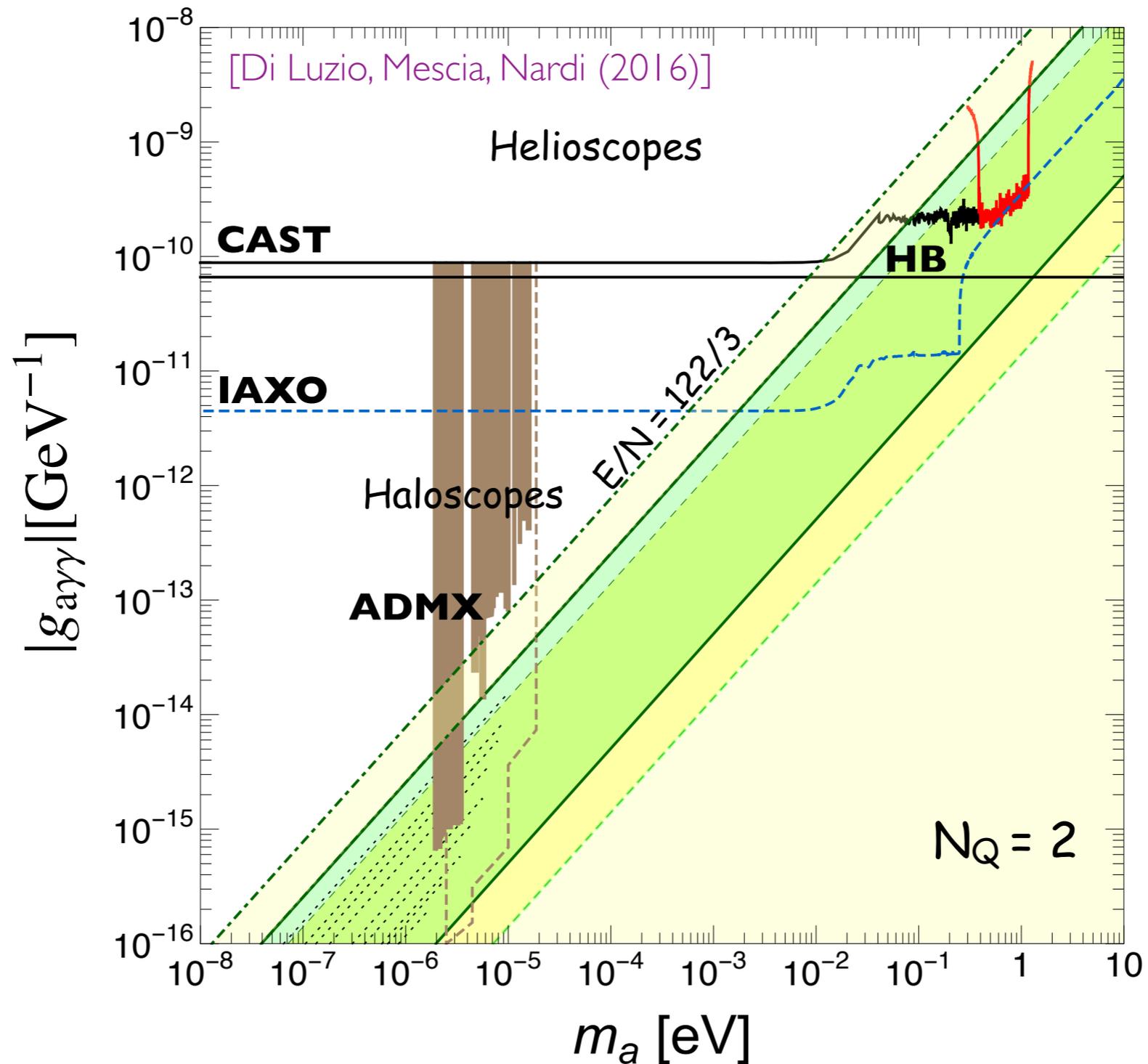
$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E_c}{N_c} - 1.92(4) \right)$$

[Theoretical error from NLO χ PT
Grilli di Cortona et al., 1511.02867]

More Q's



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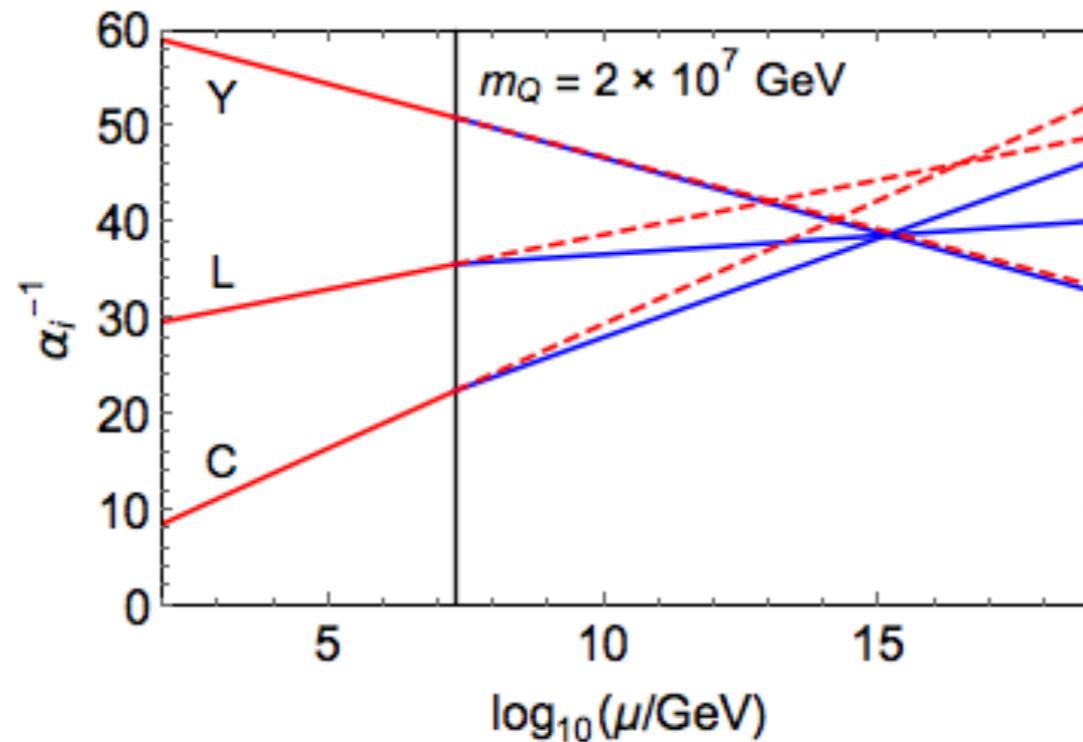
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- Here: axion window defined through precise pheno requirements.

Backup slides

Unificaxion ?

- Some Q's might improve gauge coupling unification [Giudice, Rattazzi, Strumia, 1204.5465]
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 - out of all our 15 cases, just one works fine: $Q \sim (3, 2, 1/6)$
- Conceiving a UV model remains, however, a challenge
 - $Q \in \psi_{\text{GUT}}$
 - $m_Q \lesssim f_a \ll M_{\text{GUT}}$

$$[\text{PQ}, \text{GUT}] = 0$$



$$m_{\psi_{\text{GUT}}} = \mathcal{O}(f_a)$$

- a complete GUT multiplet doesn't help !

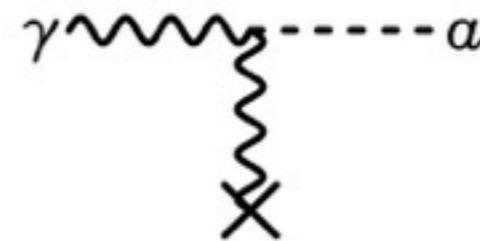
Experimental axion searches

- Many different ways to search for axions:
 - Haloscopes (axion DM)
 - Helioscopes (axions from the Sun)
 - Astrophysical bounds
 - New ideas...

Haloscopes

- Look for DM axions with a microwave resonant cavity [Sikivie (1983)]
 - exploits Primakoff effect: axion-photon transition in external static E or B field

$$\mathcal{L}_{a\gamma\gamma} = -\frac{1}{4}g_{a\gamma\gamma} a F \cdot \tilde{F} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$



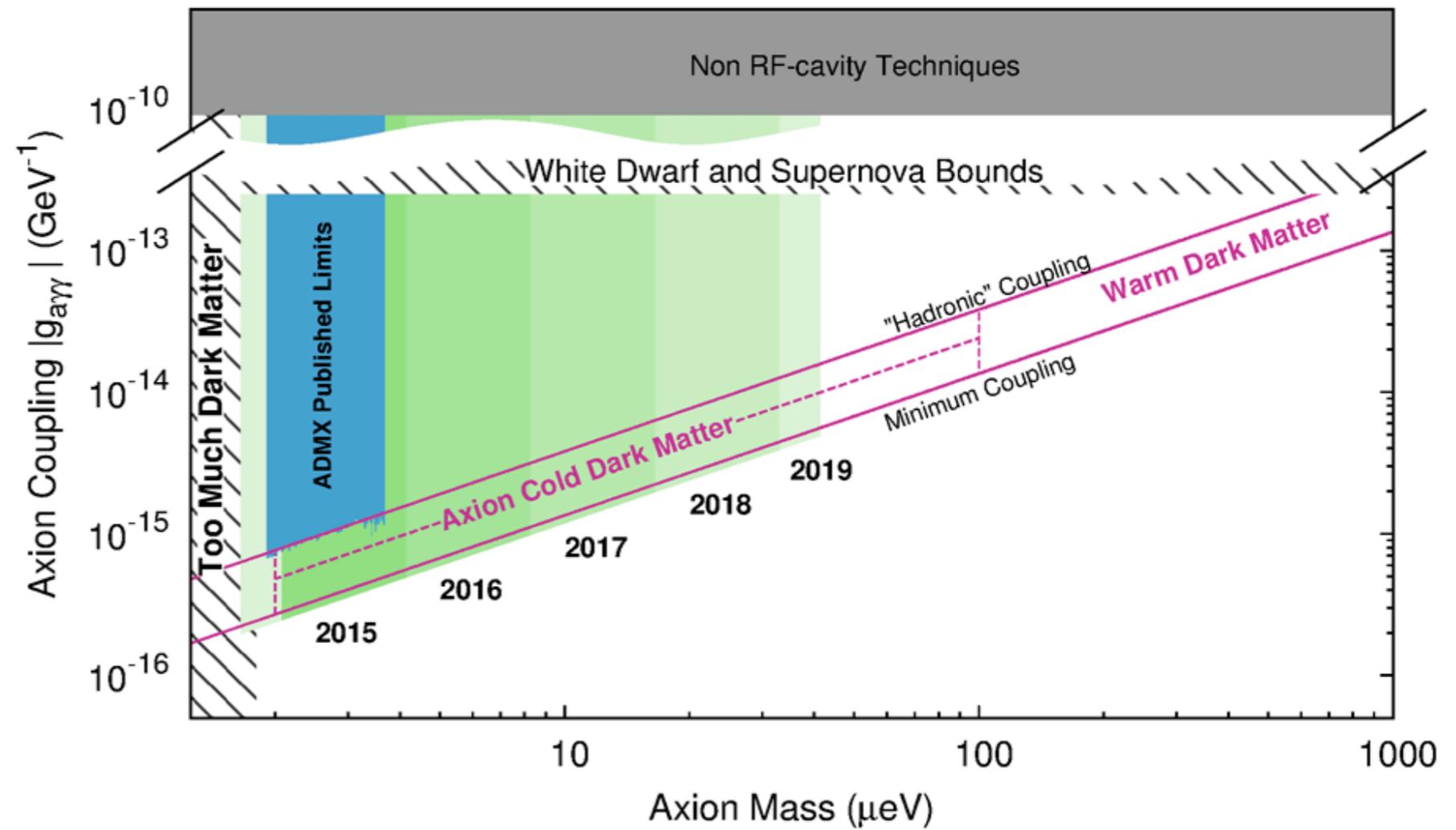
- power of axions converting into photons in an EM cavity

$$P_a = C g_{a\gamma\gamma}^2 V B_0^2 \frac{\rho_a}{m_a} Q_{\text{eff}}$$

- resonance condition: need to tune the frequency of the EM cavity on the axion mass

Haloscopes

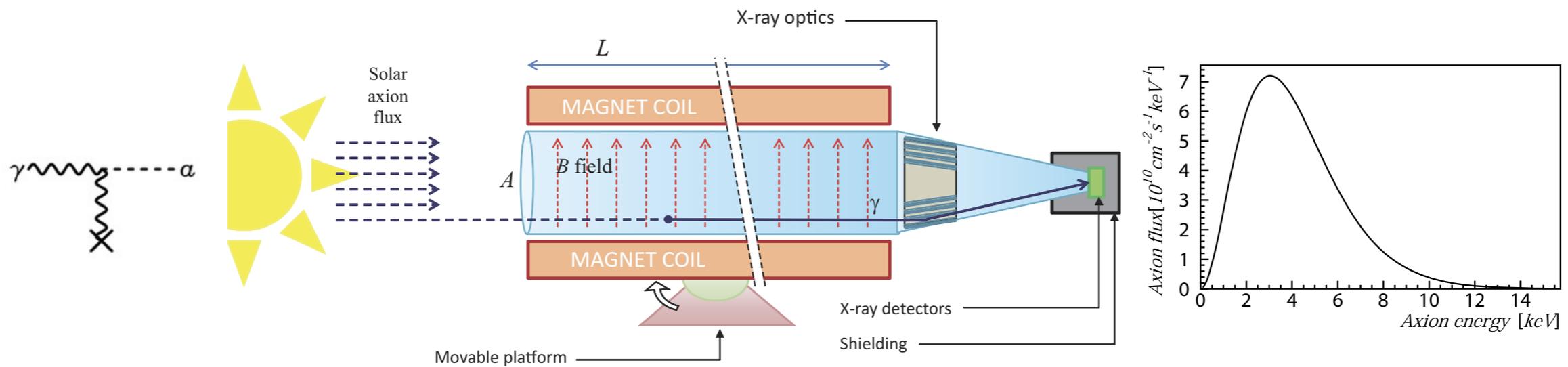
- Look for DM axions with a microwave resonant cavity
 - Axion Dark Matter eXperiment (ADMX) (U. of Washington)



[ADMX Collaboration, 0910.5914]

Helioscopes

- The Sun is a potential axion source



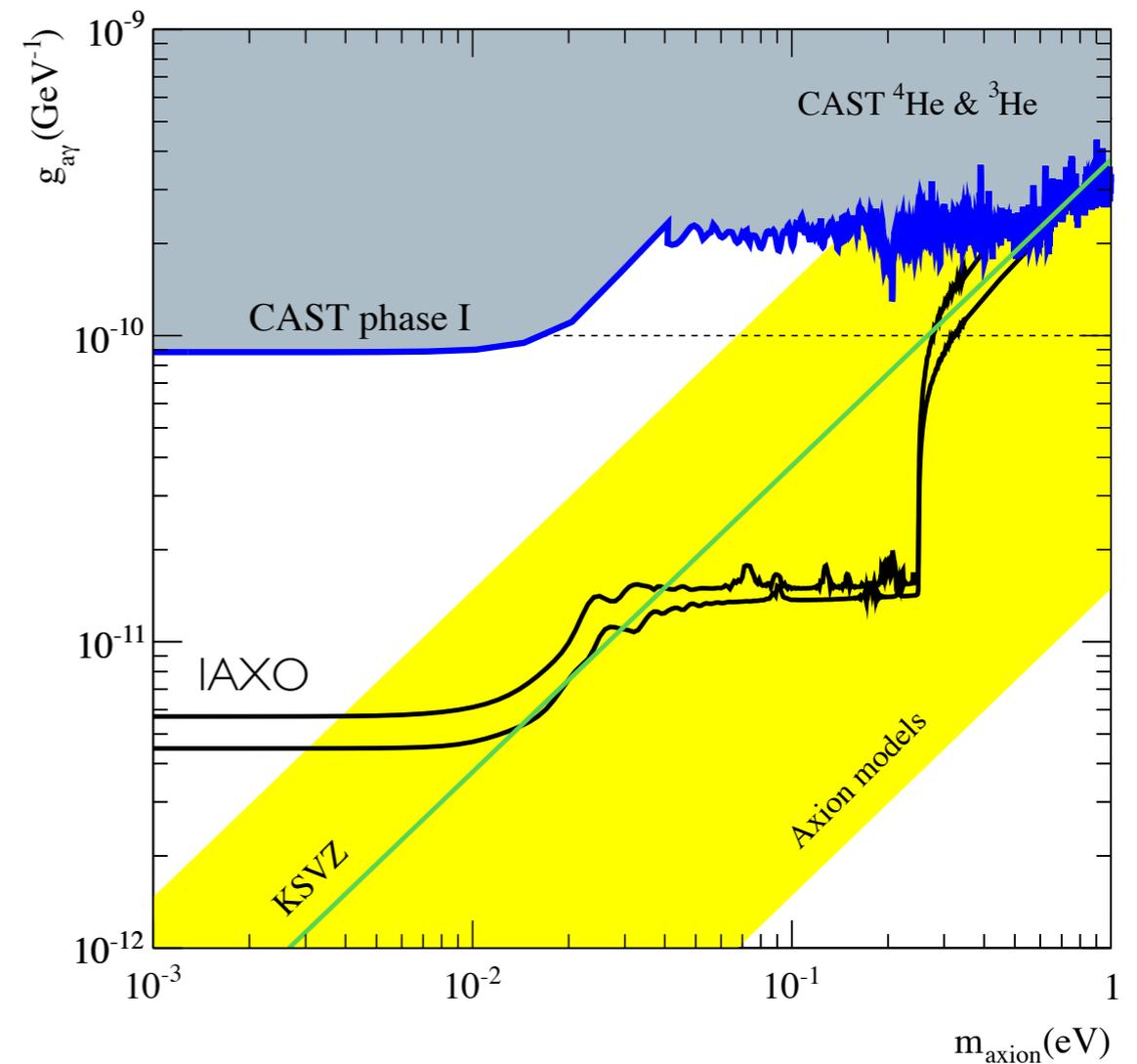
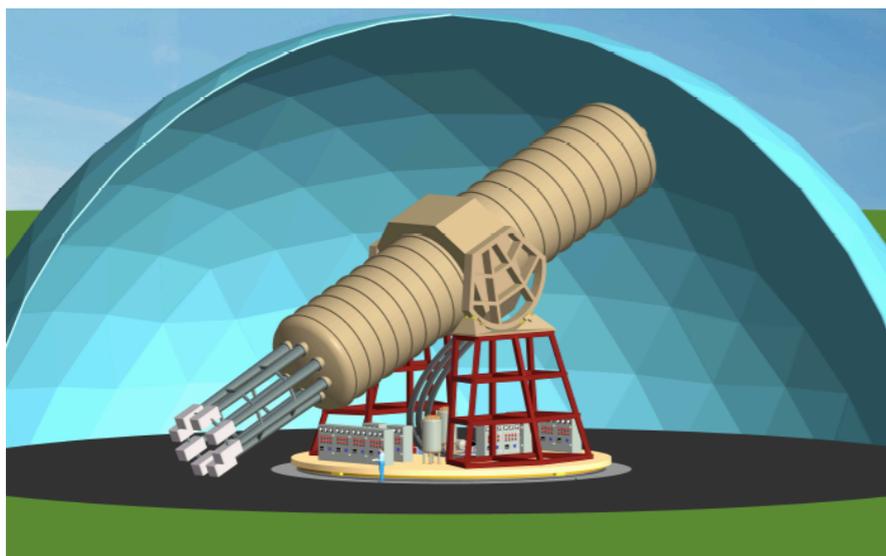
- macroscopic B-field can provide a large coherent transition rate over a big volume

Helioscopes

- The Sun is a potential axion source
 - CERN Axion Solar Telescope (CAST)



- International AXion Observatory (IAXO)



[IAXO "Letter of intent", CERN-SPSC-2013-022]

Axion couplings to photons

- Axion mass

$$m_a^2 = \frac{m_u m_d}{(m_u + m_d)^2} \frac{m_\pi^2 f_\pi^2}{f_a^2} \qquad m_a \simeq m_\pi \frac{f_\pi}{f_a} \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$$

$$g_{a\gamma\gamma} = \frac{\alpha_{em}}{2\pi f_a} \left[\frac{E}{N} - \frac{2}{3} \frac{4m_d + m_u}{m_d + m_u} \right] = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E}{N} - 1.92(4) \right)$$



EM anomaly



long distance QCD

EDM of the neutron

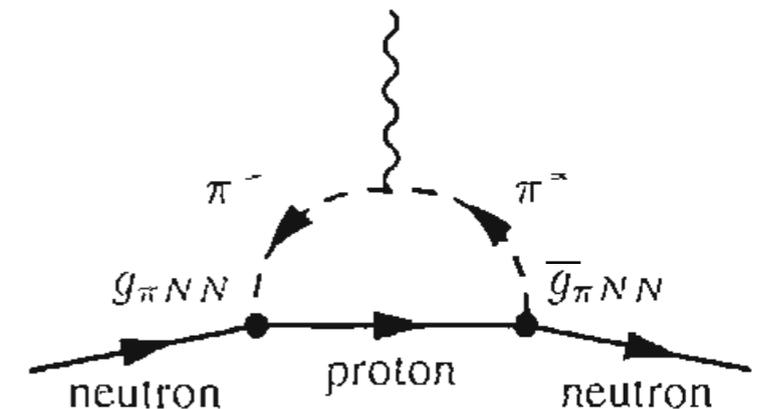
- Estimate from the nucleon-pion effective lagrangian

$$\mathcal{L}_{\pi NN} = \pi^a \bar{\Psi} (i\gamma^5 g_{\pi NN} + \bar{g}_{\pi NN}) \tau^a \Psi$$

$$g_{\pi NN} = 13.4$$

$$\bar{g}_{\pi NN} = \frac{2m_s m_u m_d}{f_\pi (m_u + m_d)} (M_\Xi - M_N) \bar{\theta} \approx 0.04 \bar{\theta}$$

[Crewther et al. (1979)]



$$d_N = \frac{m_N}{4\pi^2} g_{\pi NN} \bar{g}_{\pi NN} \ln \frac{m_N}{m_\pi} = (5.2 \times 10^{-16} e \cdot \text{cm}) \bar{\theta}$$

$$|d_N| < 2.9 \times 10^{-26} e \cdot \text{cm}$$



$$\bar{\theta} < 10^{-10}$$

A threat to the PQ solution

- “Folk’s theorem” on the non-existence of global symmetries in quantum gravity
 - global charges can be eaten by black holes, which may subsequently evaporate

[Bekenstein (1972), Zeldovich (1977)]

- Parametrizing explicit breaking by effective operators:

$$\mathcal{O}_{PQ} = k \frac{\phi^n}{\Lambda^{n-4}} \xrightarrow{SSB} |k| \frac{f^n}{\Lambda^{n-4}} \cos(na + \arg k),$$

[Kamionkowski, March-Russell (1992), Holman et al. (1992), Barr, Seckel (1992)]

- for $\Lambda = m_{Pl}$ and $f = 10^9$ GeV :

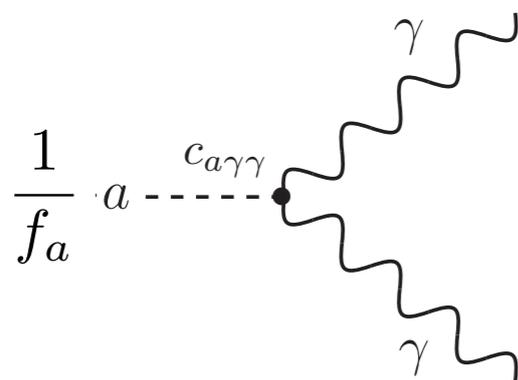
$$\bar{\theta} \lesssim 10^{-10} \quad \longrightarrow \quad n \geq 10$$

Axion couplings at low energy

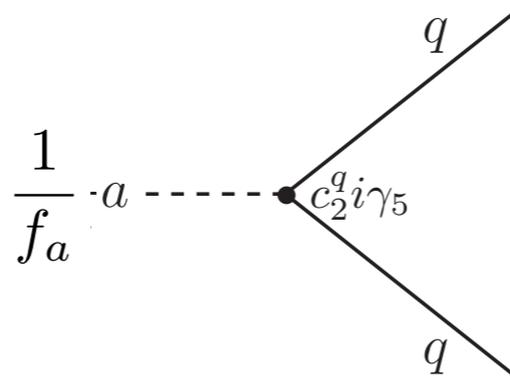
- Axion mass

$$m_a \simeq m_\pi \frac{f_\pi}{f_a} \simeq 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$$

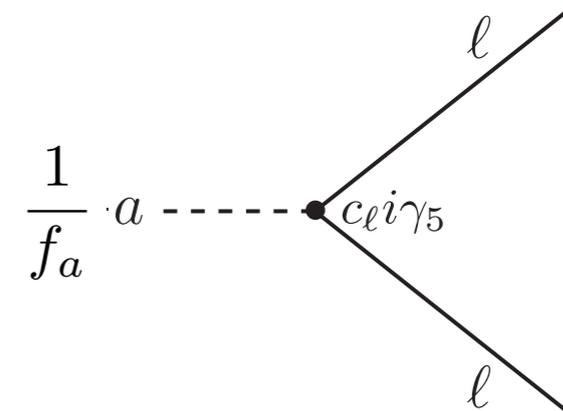
- Axion couplings



photons



hadrons



leptons

- the lighter the axion, the more weakly interacting